

# MAP-i 2007/08

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Program Semantics, Verification, and Construction  
Approaches to Correct Software

DCCFCUP / DIUM

# Motivation...

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*“Despite 50 years of progress, the software industry remains years – perhaps decades – short of the mature engineering discipline required to meet the needs of an information-age society.”*

W. Gibbs, in Trends in Computing: Software’s Chronic Crisis  
Scientific American, 1994

# Formal Methods

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- Specification and Models:  
algebraic; abstract state machines; automata; set-theoretical;  
declarative
- Theorem Proving and Proof Assistants
- Model Checking
- Hoare Logic / Weakest-precondition Calculi
- Integrated Design Methods (B)
- Refinement and Derivation of Implementations

# Goals: Not a Formal Methods Course!

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- To cover the fundamental theoretical bases of Programming Languages (Part I)
- To give an overview of some modern rigorous methods for the design of reliable software systems
  - The Logic-based approach:  
Program Verification Methods; Design by Contract (Part II)
  - The Algebraic approach:  
Program Construction and Calculation (Part III)
- NOT COVERED: Complexity theory, Computability

# Recent Changes

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- ISO-15408 (Common Criteria). Highest Evaluation Assurance levels (EAL5 – EAL7) require public certification and the use of formal methods
- Advances in the theory: correct-by-construction school of programming
- New safety requirements: code mobility ; memory confinement ; component outsourcing. GLOBAL COMPUTING
- New open standards: the JML effort; new practical and easy-to-use tools bring certification to the common programmer: Spec#, ESC/Java
- New pragmatic techniques and architectures for the certification of code: design-by-contract; proof-carrying code; certifying compilation
- Many recent success stories in industry

# The Team and Context

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- José Bacelar Almeida (DIUM)
  - Sabine Broda (DCCFCUP)
  - Luís Damas (DCCFCUP)
  - Mário Florido (DCCFCUP)
  - Maria João Frade (DIUM)
  - Nelma Moreira (DCCFCUP)
  - José Nuno Oliveira (DIUM)
  - Jorge Sousa Pinto (DIUM)
- Ongoing collaboration between DCCFCUP and DIUM
  - Recently approved joint project “RESCUE”  
(REliable and Safe Code execUtion for Embedded systems)
  - Team members are or have been members of major EC-funded networks in the area: APPSEM II, TYPES

# Part I: Overview of Foundations (15 hours)

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1. Intuitionistic logic
2. Natural deduction
3.  $\lambda$ -calculus (terms, reduction, the Church-Rosser Theorem)
4. Simple Types (Church versus Curry typing, normalization, extensions)
5. The Curry-Howard isomorphism
6. Introduction to operational semantics
7. Domain theory (complete partial orders, continuous functions)
8. Denotational semantics

# Part II: Program Verification (18 hours)

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1. Dependent Types
2. Type-based proof assistants and interactive proof development
3. Verification of the correctness of functional programs
4. Axiomatic semantics of imperative programs: Hoare Logic
5. Weakest-precondition calculi and Design-by-contract: the JML effort
6. Tool support: verification condition generators; extended static checkers
7. Survey of alternative approaches to program verification:  
Certifying compilation and proof-carrying code



# Part III: Program Construction (15 hours)

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1. Introduction to the mathematics of program construction
2. Description versus calculation
3. The Point-free (PF) transform
4. Universal properties and Galois connections;  
Reynolds' relation and the free-theorem of polymorphism
5. Reasoning by PF-calculation  
Data-level calculation: representing and abstracting data models.
6. Inductive program calculation
7. Open issues and hot topics in the mathematics of program construction

# Methods and Assessment

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- Lectures
- Tool Demonstrations / Case studies
- Exams
- Research Assignments
  - talks (read papers)
  - practical assignments